

# Hexadecimal a [learn.sparkfun.com](http://learn.sparkfun.com) tutorial

Available online at: <http://sfe.io/t210>

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## Introduction

Have you ever felt constrained forming numbers with just 10 numerical digits? Or wanted to represent large numbers with fewer digits? Or easily identify byte values without having to look at binary's hypnotic string of 1's and 0's? For applications like these, hexadecimal often becomes the engineer's number-system-of-choice.

```
Offset(h) 00 01 02 03 04 05 06 07 08 09 0A 0B 0C 0D 0E 0F
00000660 48 65 6C 6C 6F 2C 20 77 6F 72 6C 64 2E 36 34 30 Hello, world.640
00000670 30 39 30 39 31 36 35 30 30 30 31 39 36 32 33 0D 090916500019623.
00000680 0A 3A 31 30 31 45 35 30 30 30 39 30 39 33 36 35 .:101E5000909365
00000690 30 30 38 30 39 33 36 34 30 30 32 46 35 46 33 46 00809364002F5F3F
000006A0 34 46 38 30 39 31 36 36 30 31 45 46 0D 0A 3A 31 4F80916601EF.:1
000006B0 54 68 69 73 20 69 73 20 61 20 68 65 78 61 64 65 This is a hexade
000006C0 63 69 6D 61 6C 20 74 75 74 6F 72 69 61 6C 21 46 cimal tutorial!F
000006D0 38 39 34 45 31 39 39 33 36 0D 0A 3A 31 30 31 45 894E19936.:101E
000006E0 37 30 30 30 00 01 02 03 04 05 06 07 08 09 0A 0B 7000.....
000006F0 0C 0D 0E 0F 10 11 12 13 14 15 16 17 18 19 1A 1B .....
00000700 1C 1D 1E 1F 20 21 22 23 24 25 26 27 28 29 2A 2B .... !"#%&'()*+
00000710 2C 2D 2E 2F 30 31 32 33 34 35 36 37 38 39 3A 3B ,-. /0123456789.;
00000720 3C 3D 3E 3F 40 41 42 43 44 45 46 47 48 49 4A 4B <=>?@ABCDEFGHIJK
00000730 4C 4D 4E 4F 50 51 52 53 54 55 56 57 58 59 5A 5B LMNOPQRSTUVWXYZ[
00000740 5C 5D 5E 5F 60 61 62 63 64 65 66 67 68 69 6A 6B \]^_`abcdefghijk
00000750 6C 6D 6E 6F 70 71 72 73 74 75 76 77 78 79 7A 7B lmnopqrstuvwxyz{
00000760 7C 7D 7E 7F 80 81 82 83 84 85 86 87 88 89 8A 8B |}~.€.,f,,,†‡`%Š<
00000770 8C 8D 8E 8F 90 91 92 93 94 95 96 97 98 99 9A 9B Œ.Ž...''""*--™$;
00000780 9C 9D 9E 9F A0 A1 A2 A3 A4 A5 A6 A7 A8 A9 AA AB œ.žŸ ¡¢£¥¦§¨©ª«
00000790 AC AD AE AF B0 B1 B2 B3 B4 B5 B6 B7 B8 B9 BA BB ¬.®¯°±²³´µ¶·¸¹º»
000007A0 BC BD BE BF C0 C1 C2 C3 C4 C5 C6 C7 C8 C9 CA CB %&'()*+,-./:;<=>?@A
000007B0 CC CD CE CF D0 D1 D2 D3 D4 D5 D6 D7 D8 D9 DA DB IIIIÐN00000x0UUU
000007C0 DC DD DE DF E0 E1 E2 E3 E4 E5 E6 E7 E8 E9 EA EB ÜYPBääääääæçèéêë
000007D0 EC ED EE EF F0 F1 F2 F3 F4 F5 F6 F7 F8 F9 FA FB iiiiðñóôõö÷øùúû
000007E0 FC FD FE FF B3 39 43 0D 0A 3A 31 30 31 45 44 30 üýþÿ39C.:101ED0
000007F0 30 30 35 37 30 30 45 38 39 35 33 32 39 36 30 32 005700E895329602
```

Once you understand hex, the next step is decoding the matrix!

Hexadecimal -- also known as **hex** or **base 16** -- is a system we can use to write and share

numerical values. In that way it's no different than the most famous of numeral systems (the one we use every day): decimal. Decimal is a base 10 number system (perfect for beings with 10 fingers), and it uses a collection of 10 unique digits, which can be combined to positionally represent numbers.

Hex, like decimal, combines a set of digits to create large numbers. It just so happens that hex uses a set of **16 unique digits**. Hex uses the standard 0-9, but it also incorporates six digits you wouldn't usually expect to see creating numbers: A, B, C, D, E, and F.

There are many (infinite!) other numeral systems out there. [Binary](#) (base 2) is also popular in the engineering world, because it's the language of computers. The base 2, binary, system uses just two digit values (0 and 1) to represent numbers.

Hex, along with decimal and binary, is one of the most commonly encountered numeral systems in the world of electronics and programming. It's important to understand how hex works, because, in many cases, it makes more sense to represent a number in base 16 than with binary or decimal.

## Covered in This Tutorial

This tutorial covers everything hex-related that you might encounter in electronics or programming. It's split into the following sections:

- [Hex Basics](#) -- An overview of hex. This page covers the 16 digits of hex, how we represent hex numbers, and how to **count** in hex.
- [Converting To/From Decimal](#) -- This page covers our preferred methods of converting between hex and decimal.
- [Converting To/From Binary](#) -- This page shows how you can convert between binary and hex.
- [Conversion Calculators](#) -- Here you'll find a simple, automatic calculator to switch between hex, binary, and decimal.

## Suggested Reading

You should know a thing or two about decimal numbers before delving into this tutorial. Remember long division? Remainders? Quotients? Products? Sums? Exponents? Those all come back to haunt you when you're learning about hexadecimal and its relationship to decimal.

Beyond brushing up on your arithmetic, we'd recommend reading through our [binary tutorial](#) before (or along-side) this.

## Hex Basics

This page covers the very basics of hex, including an overview of the digits we use to represent hex numbers and tools we use to indicate a number is a hex value. We also cover very simple "decimal-to-hex" conversion in the form of hexadecimal counting.

## The Digits: 0-9 and A-F

Hexadecimal is a **base-16** number system. That means there are **16 possible digits** used to represent numbers. 10 of the numerical values you're probably used to seeing in decimal numbers: 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9; those values still represent the same value you're used to. The remaining six digits are represented by A, B, C, D, E, and F, which map out to values of 10, 11, 12, 13, 14, and 15.

Decimal: 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15  
 Hex: 0 1 2 3 4 5 6 7 8 9 A B C D E F

You'll probably encounter both upper and lower case representations of A-F. Both work. There isn't much of a standard in terms of upper versus lower case. *A3F* is the same number as *a3f* is the same number as *A3f*.

### Subscripts

Decimal and hexadecimal have 10 digits in common, so they can create a *lot* of similar-looking numbers. But 10 in hex is a wholly different number from that in decimal. In fact hex 10 is equivalent to decimal 16. We need a way to explicitly state whether a number we're talking about is base 10 or base 16 (or base 8, or base 2). Enter **base subscripts**:

$$16_{10} = 10_{16}$$

*Hexadecimal 10, indicated by a subscript 16, is equivalent to decimal 16 (notice the subscript 10).*

As you'll see further down, subscripts aren't the only way to explicitly state the base of a number. Subscripts are just the most literal system we can use.

### Counting in Hex

Counting in hex is a lot like counting in decimal, except there are six more digits to deal with. Once a digit place becomes greater than "F", you roll that place over to "0", and increment the digit to the left by 1.

Let's do some counting:

Decimal	Hexadecimal	...	Decimal	Hexadecimal
0	0		8	8
1	1		9	9
2	2		10	A
3	3		11	B
4	4		12	C

5	5		13	D
6	6		14	E
7	7		15	F

Once you've reached  $F_{16}$ , just as you would roll from  $9_{10}$  to  $10_{10}$  in decimal, you roll up to  $10_{16}$ :

Decimal	Hexadecimal	...	Decimal	Hexadecimal
16	10		24	18
17	11		25	19
18	12		26	1A
19	13		27	1B
20	14		28	1C
21	15		29	1D
22	16		30	1E
23	17		31	1F

And once you've reached  $1F_{16}$ , roll up to  $20_{16}$  and keep churning the right-most digit from 0 to F.

## Hex Identifiers

"BEEF, it's what's for dinner". Am I channelling my inner [Sam Elliott \(McConaughey?\)](#), or expressing my hunger for the decimal number 48879? To avoid confusing situations like that, you'll usually see a hexadecimal number prefixed (or suffixed) with one of these identifiers:

Identifier	Example	Notes
0x	0x47DE	This prefix shows up a lot in UNIX and C-based programming languages (like Arduino!).
#	#FF7734	Color references in HTML and image editing programs.
%	%20	Often used in URLs to express characters like "Space" (%20).
\x	\x0A	Often used to express character control codes like "Backspace" (\x08), "Escape" (\x1B), and "Line Feed" (\x0A).

&#x	&#x3A9	Used in HTML, XML, and XHTML to express unicode characters (e.g. &#x3A9; prints an Ω).
0h	0h5E	A prefix used by many programmable graphic calculators (e.g. TI-89).
Numeral/Text Subscript	BE37 <sub>16</sub> , 13F <sub>hex</sub>	This is more of a mathematical representation of <b>base 16</b> numbers. Decimal numbers can be represented with a subscript 10 (base 10). Binary is base 2.

There are a variety of other prefixes and suffixes that are specific to certain programming languages. Assembly languages, for example, might use an "H" or "h" suffix (e.g. 7Fh) or a "\$" prefix (\$6AD). Consult examples if you're not sure which prefix or suffix to use with your programming language.

The "0x" prefix is one you'll see a lot, especially if you're doing any [Arduino programming](#). We'll use that from now on in this tutorial.

In summary: DECAF? A horrible abomination of coffee. 0xDECAF? A perfectly acceptable, 5-digit hexadecimal number.

## Converting To/From Decimal

By now, we know how to convert about 16-or-so values between decimal and hexadecimal. To convert bigger numbers, here are some tricks we use.

### Converting Decimal to Hex

Converting from decimal to hex involves a lot of division and remainders. If you've pushed long division out of your brain, [wiki's always there](#) to help you brush up.

The steps to convert a number, let's call it  $N$ , from decimal to hex look something like this:

1. Divide  $N$  by 16. The **remainder** of that division is the first (least-significant/right-most) digit of your hex number. Take the **quotient** (the result of the division) to the next step.
  - Note: if the remainder is 10, 11, 12, 13, 14, or 15, then that becomes the hex digit A, B, C, D, E, or F.
2. **Divide the quotient** from the last step by 16 again. The remainder of this division is the **second digit** of your hex value (second-from-the-right). Take the quotient from this division to the next step.
3. Divide the quotient from step 2 by 16 again. The remainder of this division is the **third digit** of your hex conversion. Noticing a pattern?
4. Keep dividing your quotient from the last step by 16, and storing the remainder **until the result of a division is 0**. The remainder of that division is your hex value's **left-most, most-significant digit**.

## Decimal-to-Hex Example: Convert 61453

Enough math-speak, let's work an example. Let's convert  $61453_{10}$  to hexadecimal:

1. Divide 61453 by 16. The result is a **quotient of 3840**, and a **remainder of 13**. That remainder becomes our first, right-most, least-significant hex digit -- D. Take 3840 to the next step.

$$16 \overline{) 61453} \quad \begin{array}{l} \text{3840} \\ \text{R13} \sim \text{D}_{16} \end{array}$$

2. Now divide 3840 by 16. The resulting quotient is 240 with a remainder of 0. Our second hex digit is 0, and we take 240 to the next digit.

$$16 \overline{) 3840} \quad \begin{array}{l} \text{240} \\ \text{R0} \sim \text{0}_{16} \end{array}$$

3. Divide 240 by 16, and you'll get 15 with another 0 remainder. Our third hex digit is 0, and take 15 to step 4.

$$16 \overline{) 240} \quad \begin{array}{l} \text{15} \\ \text{R0} \sim \text{0}_{16} \end{array}$$

4. Finally, divide 15 by 16. That'll produce the 0 quotient we've been waiting for, with a remainder of 15. That remainder means the hex digit for this position is F.

$$16 \overline{) 15} \quad \begin{array}{l} \text{0} \\ \text{R15} \sim \text{F}_{16} \end{array}$$

Finally, **combine all four hex digits** to create our hex value: **0xF00D**.

## Converting Hex to Decimal

There's an ugly equation that rules over hex-to-decimal conversion:

$$h_n 16^n + h_{n-1} 16^{n-1} + \dots + h_1 16^1 + h_0 16^0$$

There are a few important elements to this equation. Each of the  $h$  factors ( $h_n, h_{n-1}$ ) is a **single digit** of the hex value. If our hex value is 0xF00D, for example,  $h_0$  is D,  $h_1$  and  $h_2$  are 0, and  $h_3$  is F.

**Powers of 16** are a critical part of hexadecimal. More-significant digits (those towards the left side of the number) are multiplied by larger powers of 16. The least-significant digit,  $h_0$ , is multiplied by  $16^0$  (1). If a hex value is four digits long, the most-significant digit is multiplied by  $16^3$ , or 4096.

**To convert a hexadecimal number to decimal**, you need to plug in values for each of the  $h$  factors in the equation above. Then multiply each digit by its respective power of 16, and add each product up. Our step-by-step approach is:

1. Start with the **right-most digit** of your hex value. Multiply it by  $16^0$ , that is: **multiply by 1**. In other words, leave it be, but keep that value off to the side.
  - o Remember to convert alphabetic hex values (A, B, C, D, E, and F) to their decimal equivalent (10, 11, 12, 13, 14, and 15).
2. **Move one digit to the left** Multiply that digit by  $16^1$  (i.e. **multiply by 16**). Remember that product, and keep it to the side.
3. Move another digit left. Multiply that digit by  $16^2$  (256) and store that product.
4. Continue multiplying each incremental digit of the hex value by increasing **powers of 16** (4096, 65536, 1048576, ...), and remember each product.
5. Once you've multiplied each digit of the hex value by the proper power of 16, **add them all up**. That sum is the decimal equivalent of your hex value.

### Hex-to-Decimal Example: Convert 0xC0DE

Here's an example of a four-digit hexadecimal value, 0xC0DE, that we want to convert to decimal. Creating a table and sorting the digits into separate columns can make the conversion process easier:

	Hexadecimal Digit				Notes
<b>Digit Positions</b> ( $n$ )	3	2	1	0	These values are statically assigned, they grow to the left.
<b>Hex Digits</b> Sorted	C	0	D	E	This part's easy, plug your hex values in from right-to-left.
<b>Convert A-F</b>	12	0	13	14	Convert hex values A-F to 10-15.
<b>Multiply by <math>16^n</math></b>	$12 \times 16^3$	$0 \times 16^2$	$13 \times 16^1$	$14 \times 16^0$	The exponent of 16 is the position, $n$ .
<b>Resulting</b>					

<b>Products</b>	49152	0	208	14	The product of hex digit and the power of 16.
<b>Sum Up All Products</b>	<b>49374</b>				Our decimal equivalent!

There you have it.  $CODE_{16} = 49374_{10}$ !

This table method is perfect for keeping all of your hex digits, positions, and powers-of-16 in line. To convert larger hex numbers, just add a columns to the left and increase  $n$ .

Now that you know how to do it by hand, save yourself a little time and [use a calculator](#).

## Converting To/From Binary

Breathe easy! We've gotten the hard conversions out of the way. We use hex in electrical and computer engineering because it's incredibly easy to convert to and from binary -- the 1's and 0's language of computers.

Converting between hex and binary is easy, because each digit of a hexadecimal number "maps" to **four bits** (a bit being an individual binary digit) of a binary value. **So a byte** -- eight binary digits -- can always be **represented by two hexadecimal digits**. This makes hex a really great, concise way to represent a byte or group of bytes.

### Converting from Binary to Hex

Let's begin by mapping the first 16 hexadecimal values to binary.

Decimal	Hex	Binary	...	Decimal	Hex	Binary
00	0	0000		08	8	1000
01	1	0001		09	9	1001
02	2	0010		10	A	1010
03	3	0011		11	B	1011
04	4	0100		12	C	1100
05	5	0101		13	D	1101
06	6	0110		14	E	1110
07	7	0111		15	F	1111



As you grow, and continue to use hex and binary, these 16 values will become ingrained in your brain. Those are the key to converting between hex and binary.

To convert between binary and hex, we want to take advantage of the fact that four binary digits (bits) map to one hex digit. **Follow these steps** to convert from binary to hex.

1. Split a binary value into **groups of four**, starting at the right-most side.
2. For each group of four, consult the table above to find the matching hex value, and **replace groups of four binary digits with the one hex value**.

That's it! Let's try it out.

### Binary to Hex Example: Convert 0b101111010100001

To begin, start at the far-right of the binary number, and sort the 1's and 0's into groups of four:

<b>Binary Digits Sorted:</b>	0101	1110	1010	0001
------------------------------	------	------	------	------

Now consult our big table-o'-sixteen to convert the groups-of-four to a hex digit:

<b>Binary Digits Sorted:</b>	0101	1110	1010	0001
<b>Hex Equivalents:</b>	5	E	A	1

And there you have it! 0b101111010100001 = 0x5EA1. (Ugh. This tutorial has far exceeded everyone's tolerance for [1337](#). My apologies.)

### Converting from Hex to Binary

Converting from hex to binary is a lot like converting binary to hex. Simply take a hex digit and turn it into **four binary digits**. Repeat until your number is full of 0's and 1's.

### Hex to Binary Example: Convert 0xDEADBEEF

To convert 0xDEADBEEF (a [commonly used code](#) to indicate a system crash), begin by sorting the digits into "bins":

<b>Hex Digits Sorted:</b>	D	E	A	D	B	E	E	F
---------------------------	---	---	---	---	---	---	---	---

Then convert each hex digit into four bits:

<b>Hex Digits Sorted:</b>	D	E	A	D	B	E	E	F
<b>Hex Digits Sorted:</b>	1101	1110	1010	1101	1011	1110	1110	1111

In other words, 0xDEADBEEF = 0b11011110101011011011111011101111. That's a lot of 1's and 0's.

## Use Hex to Represent and Identify Bytes

The examples above show off one of hex's greatest powers: **easily representing values of bytes**. Hex is often easier for us to work with because the values are shorter and more memorable than a long string of 1's and 0's.

Name	Slave Address	Type	Register address	
			Hex	Binary
Reserved	<i>Table 16</i>	--	00-0E	--
WHO_AM_I_G	<i>Table 16</i>	r	0F	000 1111
Reserved	<i>Table 16</i>	--	10-1F	--
CTRL_REG1_G	<i>Table 16</i>	rw	20	010 0000
CTRL_REG2_G	<i>Table 16</i>	rw	21	010 0001
CTRL_REG3_G	<i>Table 16</i>	rw	22	010 0010

For example, the register map above is from the [LSM9DS0](#) (a [nifty, 9DOF sensor](#)). It lists register addresses, which are used to control the sensor, in both hex and binary. If you want to access the CTRL\_REG2\_G register, it's much easier to remember 0x21 than 0b010001, and discovering a typo in the hex value is much easier than in binary. For that reason, we're much more likely to use hex values in our code than their binary equivalents.

## Conversion Calculators

If you're overdosing on long division, trying to convert decimal to hexadecimal, or getting lost trying to calculate powers of 16, give these calculators a try.

Entering a number into any of the boxes below will automatically update the others with the

matching value. You can type a hex value in, to convert to binary and decimal. Or type a decimal or binary number to generate a hex value. Use it as you please!

Decimal:  (0-9)

Binary:  (0-1)

Hexadecimal:  (A-F, a-f, 0-9)

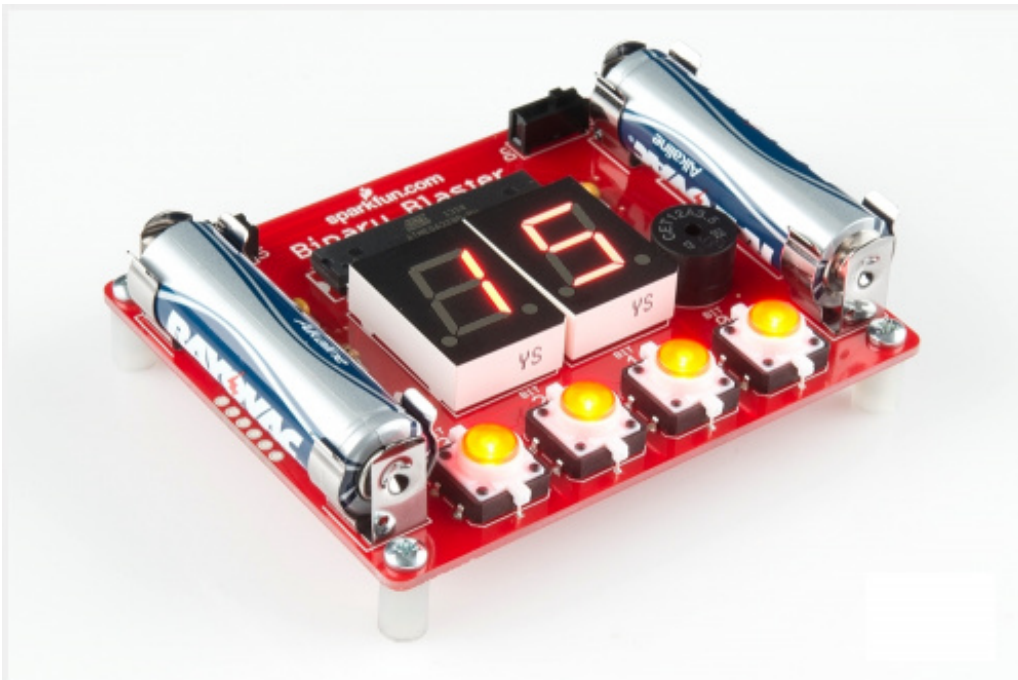
This calculator requires Javascript. If it isn't working, make sure JS is enabled (if'n you please).

## Resources and Going Further

Understanding how hexadecimal works is key to so many areas of electronics and programming.

Armed with your shiny, new hex knowledge, here are some related tutorials you may want to check out from here:

- [Digital Logic](#) and [Shift registers](#) -- These tutorials use hex as a foundation for larger, more general electronics concepts. Digital logic is the core behind all of the decision making a computer does. Shift registers can be used to fan a single input or output out to 8-or-more.
- [I<sup>2</sup>C](#) and [SPI](#) -- These communication interfaces almost always require use of hex in some way or another. Devices that communicate of SPI or I<sup>2</sup>C usually have a list of registers, which are all mapped with hexadecimal addresses. I<sup>2</sup>C devices are all assigned unique, 7-bit addresses, which are usually presented in hexadecimal.



- [Binary Blaster Hookup Guide](#) -- If you're looking to practice your hex conversions, the [Binary](#)

[Blaster Kit](#) can be a great help. This is a soldering kit. Once you've put it together, use it to test your knowledge of how binary, hex, and decimal are related.

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